

Supplementary material (Ablaut in Siyuewu Khroskyabs)

April 21, 2020

1 Introduction

The supplementary material consists of two four parts.

1. Comma-separated files
 - `allverbs.csv`: containing all the simplex verbs in the database
 - `ablauting.csv`: containing only the ablauting verbs
 - `allproto.csv`: a tentative reconstructed system (all simplex verbs)
2. Python scripts
 - `main.py`: measuring overall entropies (all vowels included) and bootstrapping
 - `ent.py`: entropy measurements
 - `bo.py`: bootstrap
 - `vmain.py`: measuring overall entropies by individual vowels
 - `vow.py`: entropy measurements
 - `bov.py`: bootstrap
3. Two folders containing results (the file names in each folder are identical)
 - `results_overall`: the results executed by `main.py`
 - `results_vowels`: the results excuted by `vmain.py`
 - `entropies_allverbs.txt`: entropies of all verbs
 - `entropies_ablauting.txt`: entropies of ablauting verbs
 - `entropies_all_proto_verbs.txt`: entropies of all reconstructed verbs
 - Folder `boot_allverbs`: bootstrap results for all verbs
 - Folder `boot_ablauting`: bootstrap results for ablauting verbs
 - Folder `charts_allverbs`: histograms and barcharts for the analyses for all verbs
 - Folder `charts_ablauting`: histograms and barcharts for the analyses for ablauting verbs
 - `results_ablauting`: the results excuted by `vmain.py`
4. The present document, which is a presentation of the supplementary material.

2 The .csv files

The .csv files data selected for the analysis, which are presented in four columns: *verb*, *s1vowel*, *s2vowel*, and *nativeness*.

1. The column *verb* contains actual verb forms.
2. The column *s1vowel* contains vowels in Stem 1.
3. The column *s2vowel* contains vowels in Stem 2.
4. The column *nativeness* contains information about the verb's nativeness: *n* means that it is a native word, and *b* means that it is a borrowing.

With a text editor, the columns are separated by commas, which are not directly and straightforwardly readable. The file can be alternatively opened by a spreadsheet application, where it appears as a spreadsheet. Table 1 shows the first few rows of the file.

Table 1: First few rows of each .csv files

verb	s1vowel	s2vowel	nativeness
zóγ	o	u	n
ληάκ	æ	æ	n
rdzáv	a	i	n
dód	o	o	b
νάκ	æ	æ	n
nlváγ	a	i	n
χπίd	i	i	n
p ^h æγλόγ	o	u	n
ts ^h ôγ	o	u	n
már	a	a	n
ttæv	æ	i	n

3 The Python scripts

3.1 ent.py and vow.py

The Python scripts (*ent.py* and *vow.py*) mainly use the library *pyitlib* which specialises in information-theoretic analyses. Its documentation can be found at the following link: <https://pafoster.github.io/pyitlib/>.

The scripts that measure entropies first modify the .csv files to make them readable by the machine. They automatically create the column *coda*, which lists the coda of each verb under the column *verb*. A part of the modified .csv file is illustrated in Table 2.

Table 2: First few rows of `sywstems.csv`

verb	s1vowel	s2vowel	nativeness	coda
<i>zóγ</i>	<i>o</i>	<i>u</i>	n	<i>γ</i>
<i>lɣǣκ</i>	<i>æ</i>	<i>æ</i>	n	<i>κ</i>
<i>rdzáv</i>	<i>a</i>	<i>i</i>	n	<i>v</i>
<i>dód</i>	<i>o</i>	<i>o</i>	b	<i>d</i>
<i>nǣκ</i>	<i>æ</i>	<i>æ</i>	n	<i>κ</i>
<i>nlváγ</i>	<i>a</i>	<i>i</i>	n	<i>γ</i>
<i>χpíd</i>	<i>i</i>	<i>i</i>	n	<i>d</i>
<i>p^hæylóγ</i>	<i>o</i>	<i>u</i>	n	<i>γ</i>
<i>ts^hôγ</i>	<i>o</i>	<i>u</i>	n	<i>γ</i>
<i>már</i>	<i>a</i>	<i>a</i>	n	<i>r</i>
<i>ftǣv</i>	<i>æ</i>	<i>i</i>	n	<i>v</i>

3.2 bo.py and bov.py

The bootstrapping scripts randomly and independently generate patterns for each entropy measurements. For each pattern, a random element is filled in a cell that allows its occurrence. The number of rows of a bootstrap sample equals to that of the corresponding observed pattern.

The reader is welcomed to test the scripts out with the original data and explore more possibilities that might be related to the predictability of the ablauting status. One can also test it out with similar data from other dialects or languages.

4 Results

4.1 Overall

All verbs:

$H(V^1 \Rightarrow V^2)$: 0.6616698383775215

$H(V^1, \text{coda} \Rightarrow V^2)$: 0.26657539306013334

$H(V^1, \text{nativeness} \Rightarrow V^2)$: 0.6225586099214304

$H(V^1, \text{coda}, \text{nativeness} \Rightarrow V^2)$: 0.24474804170852238

$H(V^2 \Rightarrow V^1)$: 0.7996850735668173

$H(V^2, \text{coda} \Rightarrow V^1)$: 0.4999384162714797

$H(V^2, \text{nativeness} \Rightarrow V^1)$: 0.7290623813473207

$H(V^2, \text{coda}, \text{nativeness} \Rightarrow V^1)$: 0.41695416679393027

Ablauting verbs:

$H(V^1 \Rightarrow V^2)$: 0.8372840491505933

$H(V^1, \text{coda} \Rightarrow V^2)$: 0.3974144721627981

$H(V^1, \text{nativeness} \Rightarrow V^2)$: 0.7892435292894153

$H(V^1, \text{coda}, \text{nativeness} \Rightarrow V^2)$: 0.3626649443708292

$H(V^2 \Rightarrow V^1)$: 0.785987669373259

$H(V^2, \text{coda} \Rightarrow V^1)$: 0.5318609377704338

$H(V^2, \text{nativeness} \Rightarrow V^1)$: 0.6527169660454337

$H(V^2, \text{coda}, \text{nativeness} \Rightarrow V^1)$: 0.4375

4.1.1 Bootstrap results for all verbs

Mean $H(V^1 \Rightarrow V^2)$: 1.2579371879406935

Variance: 0.02270362131367313

p -value = 0.0

Mean $H(V^1, \text{nativeness} \Rightarrow V^2)$: 1.1580927152532212

Variance: 0.015317236370593977

p -value = 0.0

Mean $H(V^1, \text{coda} \Rightarrow V^2)$: 0.7097702653818792

Variance: 0.00788552564162159

p -value = 0.0

Mean $H(V^1, \text{coda}, \text{nativeness} \Rightarrow V^2)$: 0.532119072416192

Variance: 0.005493763532372154

p -value = 0.0

Mean $H(V^2 \Rightarrow V^1)$: 1.2606471332654932

Variance: 0.02126351560300884

p -value = 0.0

Mean $H(V^2, \text{nativeness} \Rightarrow V^1)$: 1.1076992069806724

Variance: 0.01832645982492952

p -value = 0.0

Mean $H(V^2, \text{coda} \Rightarrow V^1)$: 0.6977541063081687
Variance: 0.00820627586998337
 p -value = 0.009

Mean $H(V^2, \text{nativeness, coda} \Rightarrow V^1)$: 0.559445546322198
Variance: 0.005530508018767922
 p -value = 0.019

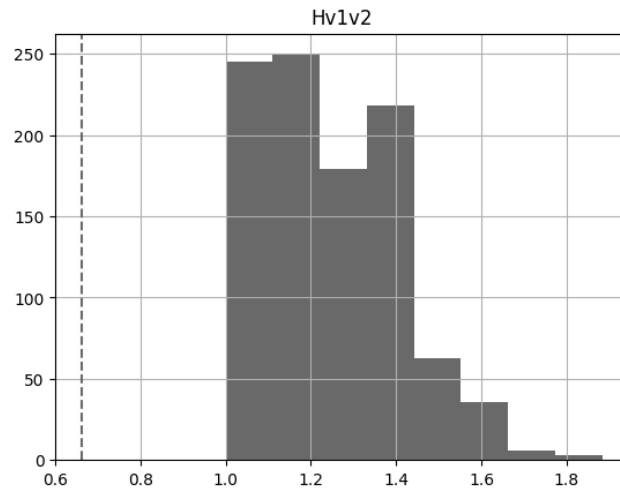


Figure 1: $H(V1 \Rightarrow V2)$

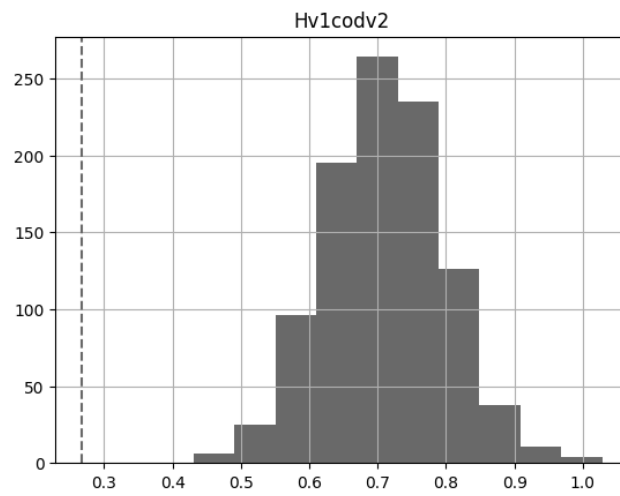


Figure 2: $H(V1, C \Rightarrow V2)$

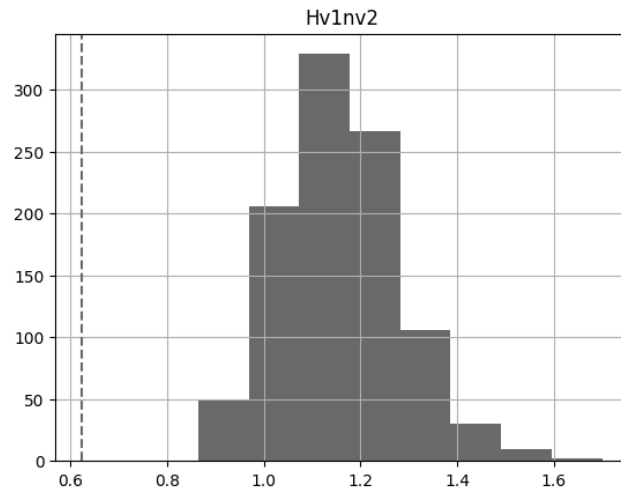


Figure 3: $H(V1, N \Rightarrow V2)$

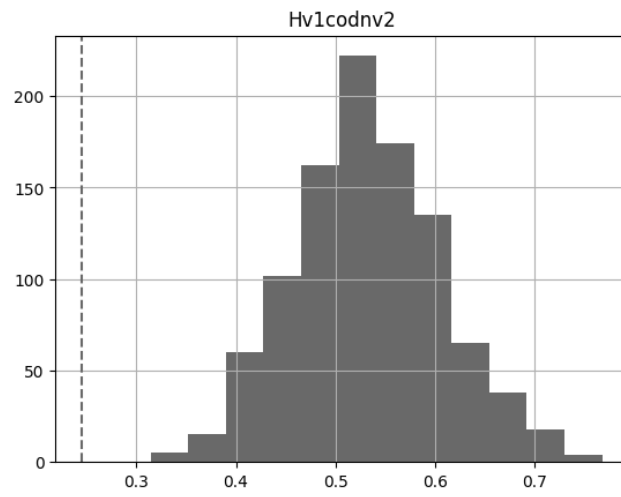


Figure 4: $H(V1, C, N \Rightarrow V2)$

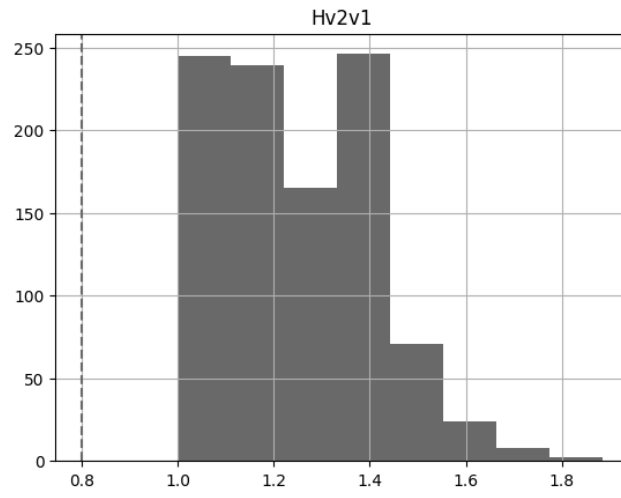


Figure 5: $H(V2 \Rightarrow V1)$

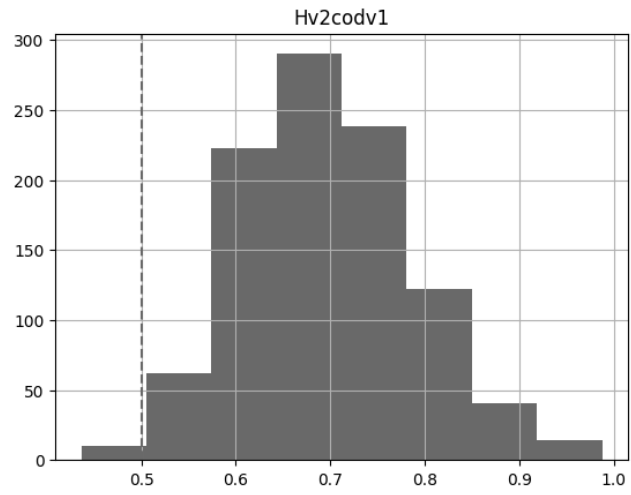


Figure 6: $H(V2, C \Rightarrow V1)$

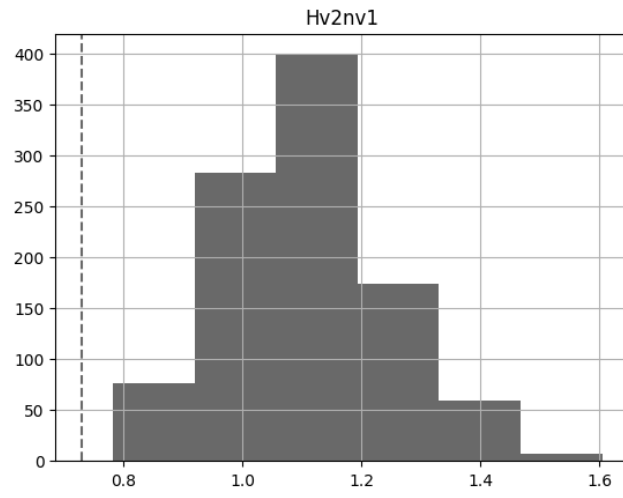


Figure 7: H(V2, C \Rightarrow V1)

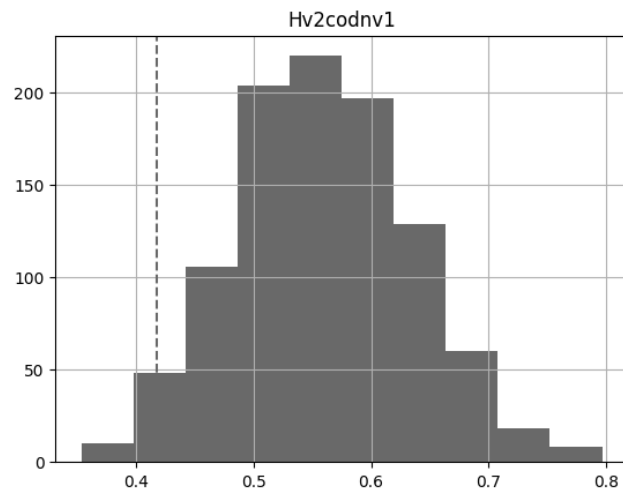


Figure 8: H(V2, C, N \Rightarrow V1)

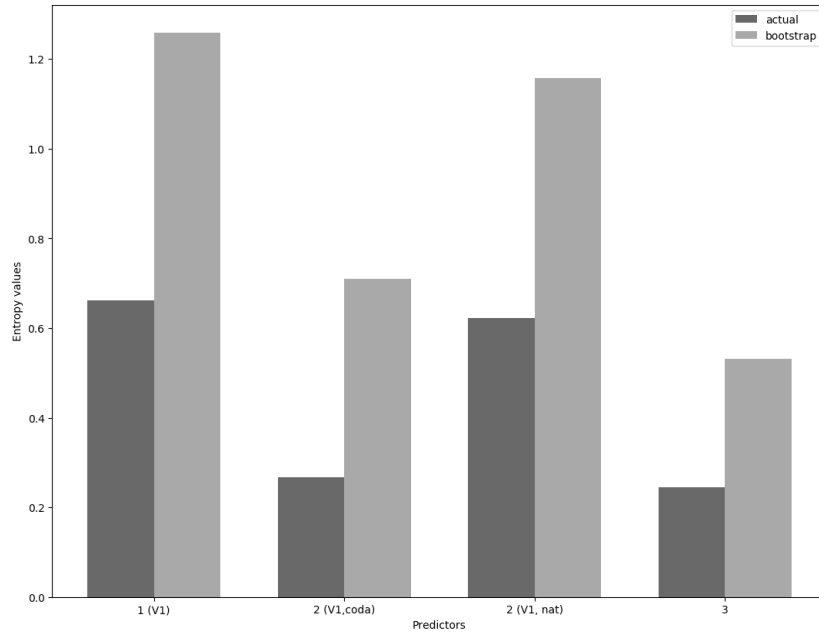


Figure 9: Comparison between mean entropies and observed ones (predicting V2)

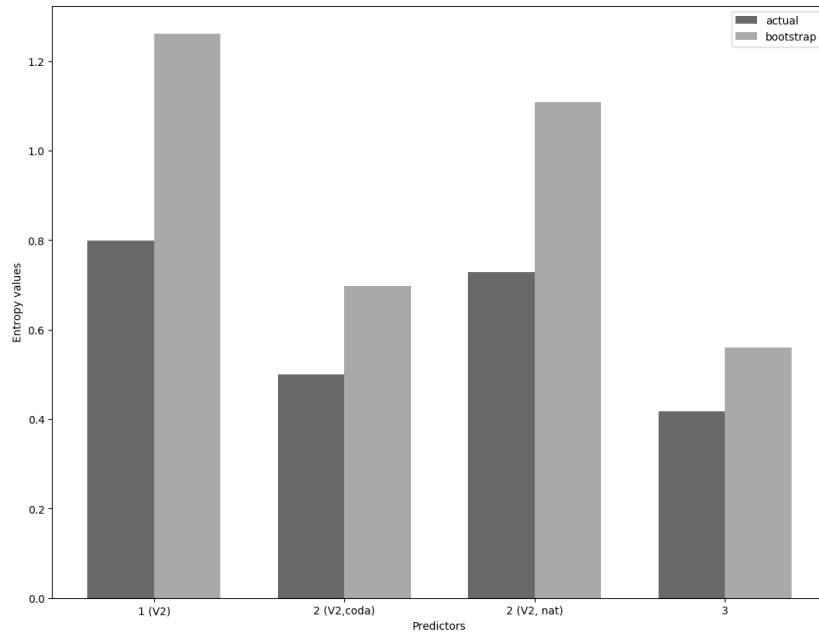


Figure 10: Comparison between mean entropies and observed ones (predicting V1)

4.1.2 Bootstrap results for ablauting verbs

Mean $H(v1 \Rightarrow v2)$: 1.327762450337501

Variance: 0.013472401247941097

p -value = 0.0

Mean $H(v1, \text{nativeness} \Rightarrow v2)$: 1.080255832659954
Variance: 0.02492476944619584
 p -value = 0.0

Mean $H(v1, \text{coda} \Rightarrow v2)$: 0.5165644844753682
Variance: 0.02138380423384964
 p -value = 0.206

Mean $H(v1, \text{coda}, \text{nativeness} \Rightarrow v2)$: 0.34479799083982815
Variance: 0.013542596098814747
 p -value = 0.558

Mean $H(v2 \Rightarrow v1)$: 0.9735519055540187
Variance: 0.021622173770458976
 p -value = 0.0

Mean $H(v2, \text{nativeness} \Rightarrow v1)$: 1.0209200263860305
Variance: 0.027339901622032255
 p -value = 0.0

Mean $H(v2, \text{coda} \Rightarrow v1)$: 0.5088586661942051
Variance: 0.018072736150108803
 p -value = 0.569

Mean $H(v2, \text{nativeness}, \text{coda} \Rightarrow v1)$: 0.2470562984485877
Variance: 0.010325904743142822
 p -value = 0.955

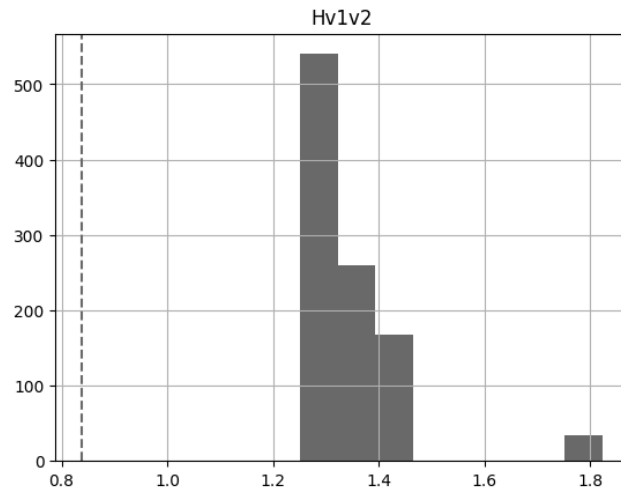


Figure 11: $H(V1 \Rightarrow V2)$

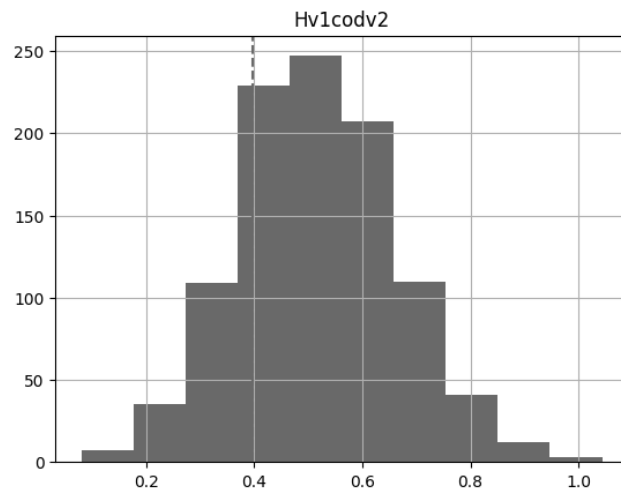


Figure 12: $H(V1, C \Rightarrow V2)$

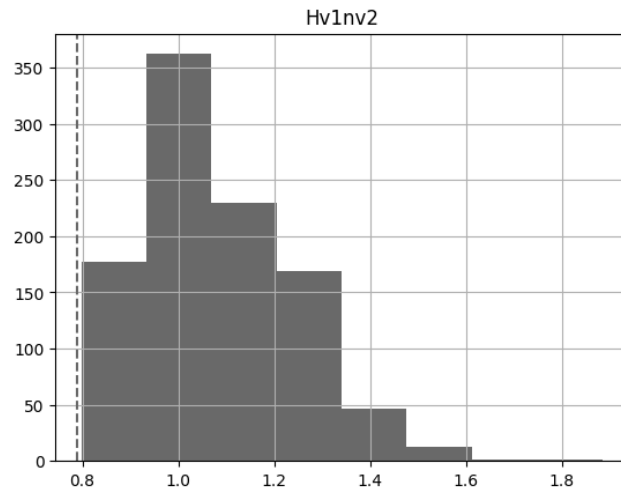


Figure 13: $H(V1, N \Rightarrow V2)$

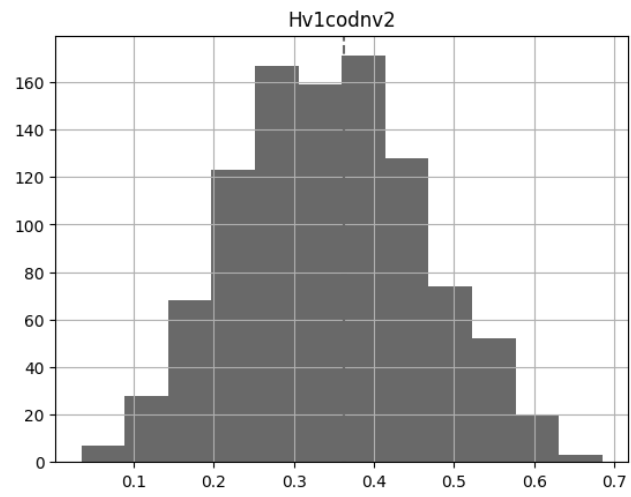


Figure 14: $H(V1, C, N \Rightarrow V2)$

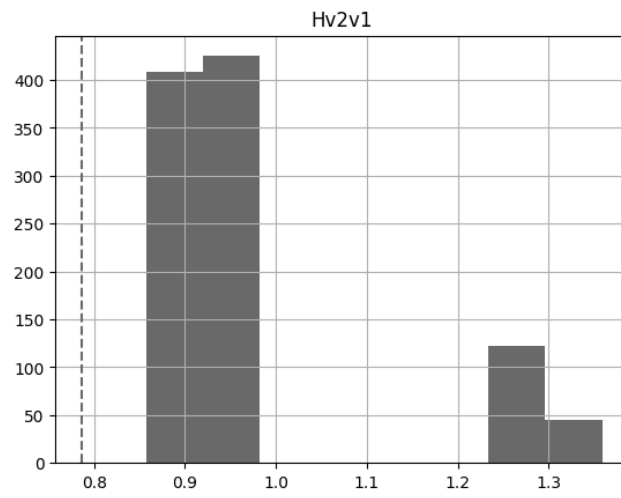


Figure 15: $H(V2 \Rightarrow V1)$

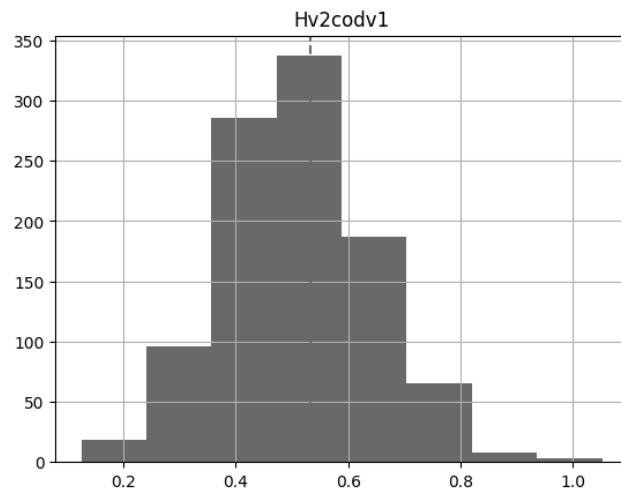


Figure 16: $H(V2, C \Rightarrow V1)$

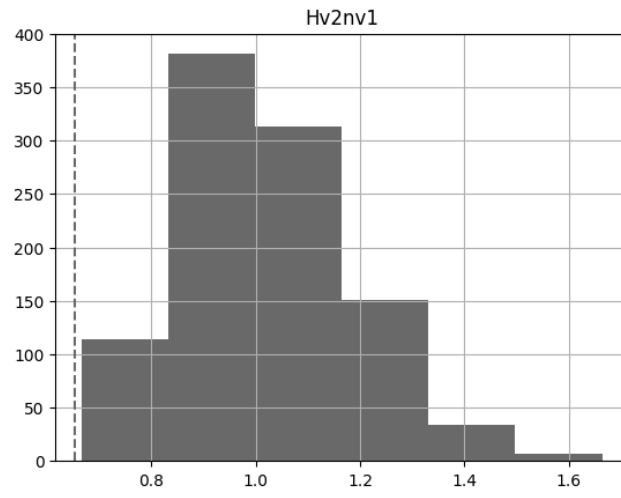


Figure 17: H(V2, C \Rightarrow V1)

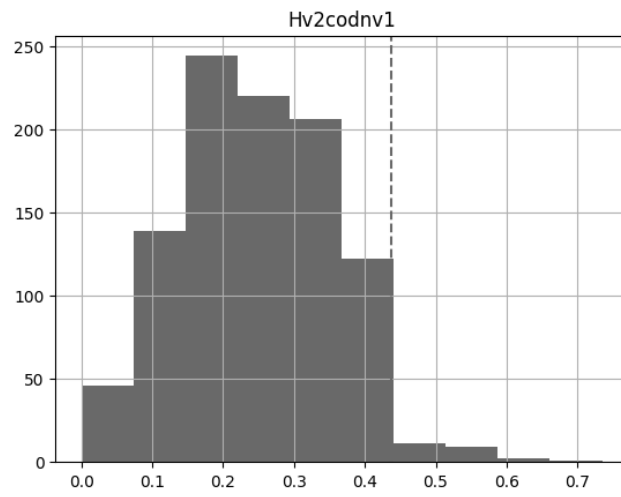


Figure 18: H(V2, C, N \Rightarrow V1)

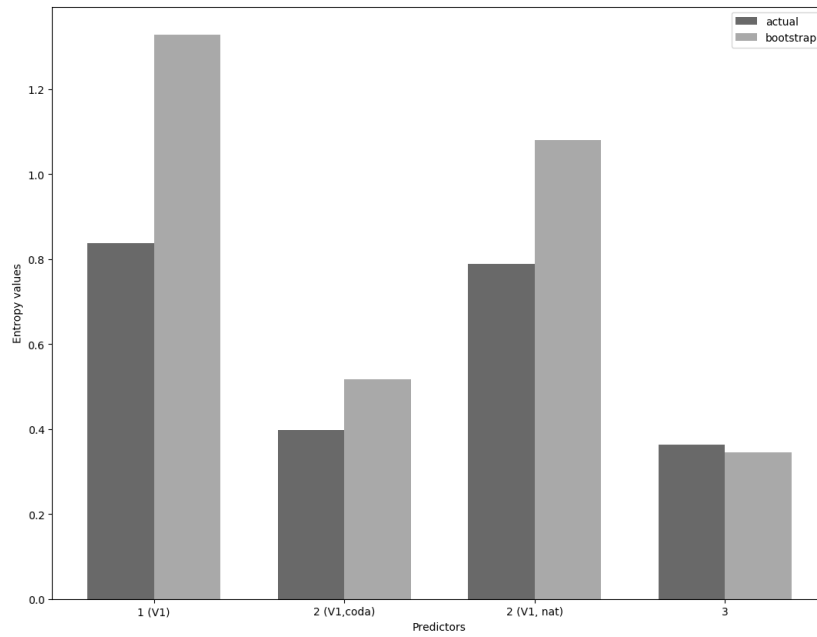


Figure 19: Comparison between mean entropies and observed ones (predicting V2)

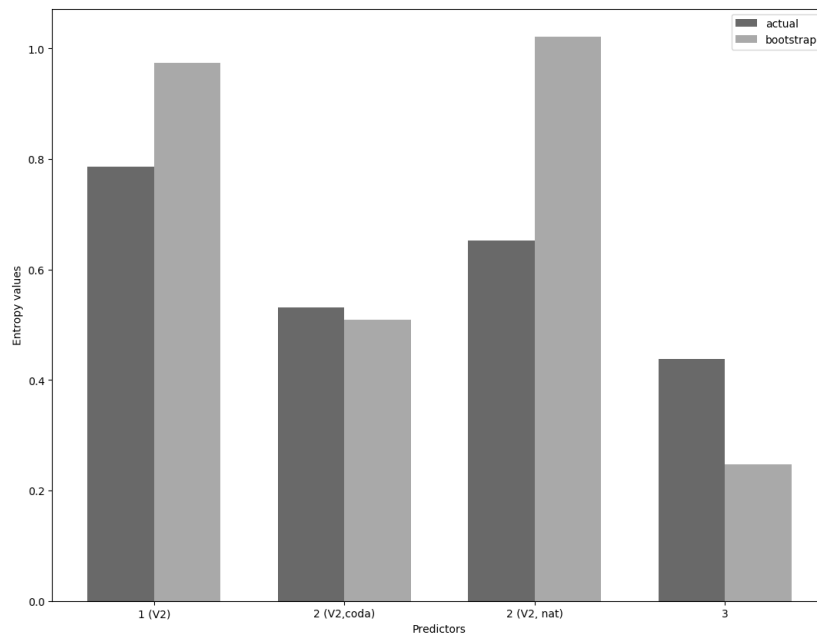


Figure 20: Comparison between mean entropies and observed ones (predicting V1)

4.2 By individual vowel

All verbs:

H(æ, coda, nativeness => V2): 0.8994903523161897
H(a, coda, nativeness => V2): 0.30264355998510517
H(o, coda, nativeness => V2): 0.14885837146039105
H(i, coda, nativeness => V1): 0.7930308751537449
H(ə, coda, nativeness => V1): 0.3670548003099765
H(u, coda, nativeness => V1): 0.3984289271052721
H(o,coda,nativeness => V1): 0.03773584905660399

Ablauting verbs:

H(æ, coda, nativeness => V2): 0.805922098601842
H(a, coda, nativeness => V2): 0.0
H(o, coda, nativeness => V2): 0.0
H(i, coda, nativeness => V1): 0.5895477321576896
H(ə, coda, nativeness => V1): 0.30348723565334224
H(u, coda, nativeness => V1): 0.2516606809315953
H(o,coda,nativeness => V1): 0.0

4.2.1 Bootstrap results for all verbs

Mean H(æ, coda, nativeness => v2): 2.1283065522258147
Variance: 0.003669831616213124
 p -value = 0.0

Mean H(a, coda, nativeness => V2): 1.7840531661498096
Variance : 0.00550022949649929
 p -value = 0.0

Mean H(o, coda, nativeness => v2): 2.0146897241662485
Variance: 0.004306399148803152

p -value = 0.0

Mean $H(i, \text{coda}, \text{nativeness} \Rightarrow v1)$: 2.1038750443878773

Variance: 0.0036585654480020637

p -value = 0.0

Mean $H(\text{ə}, \text{coda}, \text{nativeness} \Rightarrow v1)$: 2.344455826599742

Variance: 0.0024606953067613105

p -value = 0.0

Mean $H(u, \text{coda}, \text{nativeness} \Rightarrow v1)$: 1.8647004759665824

Variance: 0.005277167986595714

p -value = 0.0

Mean $H(o, \text{coda}, \text{nativeness} \Rightarrow v1)$: 1.3942468687939618

Variance: 0.00941975368204351

p -value = 0.0

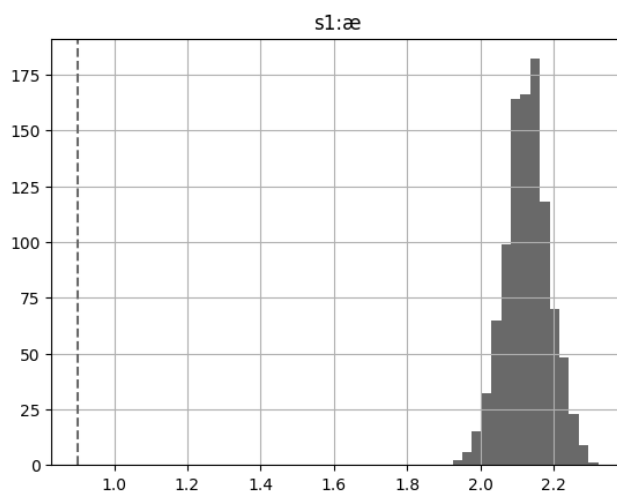


Figure 21: $H(\text{æ}, C, N \Rightarrow V2)$

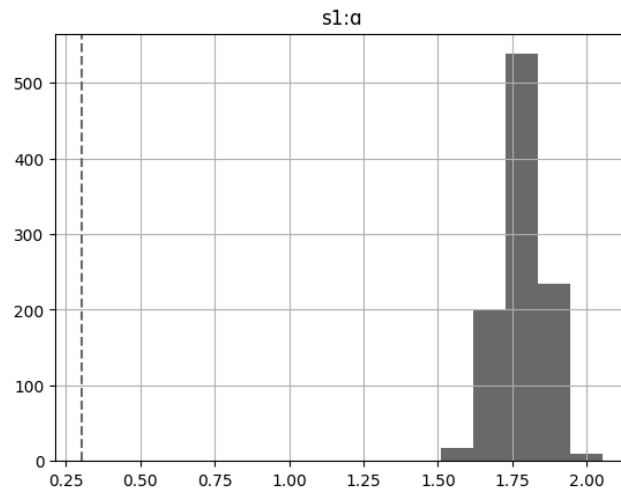


Figure 22: $H(a, C, N \Rightarrow V2)$

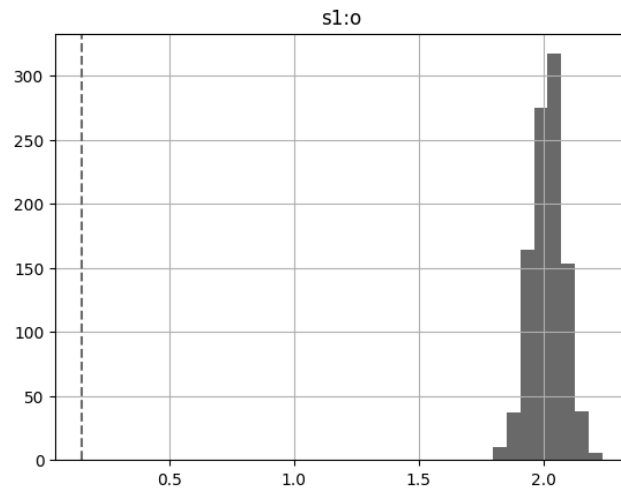


Figure 23: $H(o, C, N \Rightarrow V2)$

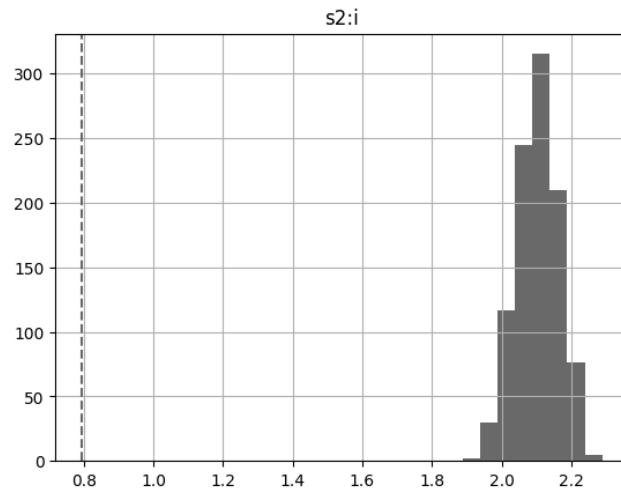


Figure 24: $H(i,C,N \Rightarrow V1)$

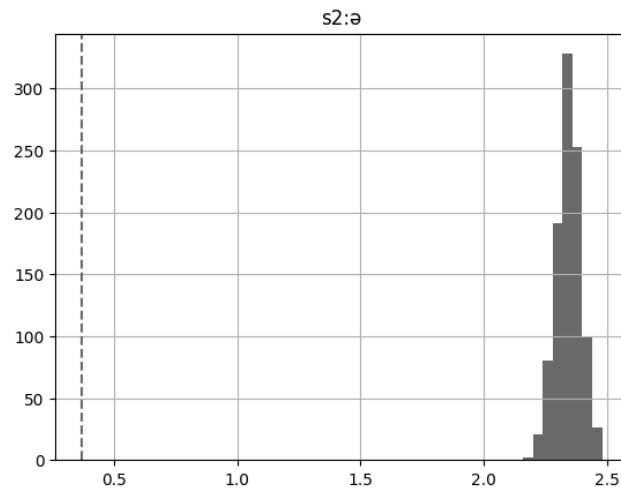


Figure 25: $H(ə,C,N \Rightarrow V1)$

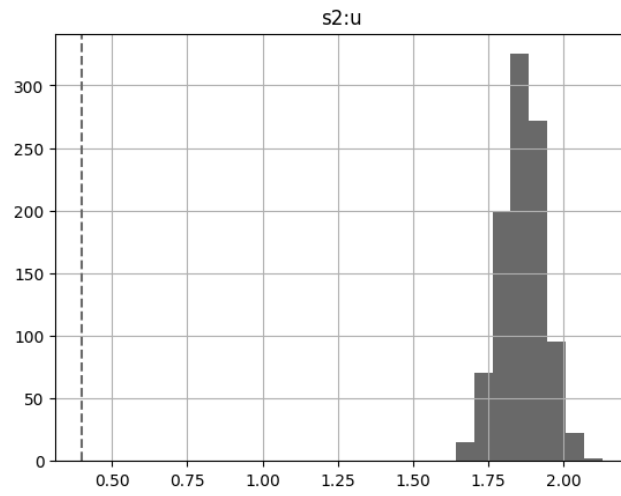


Figure 26: $H(u, C, N \Rightarrow V1)$

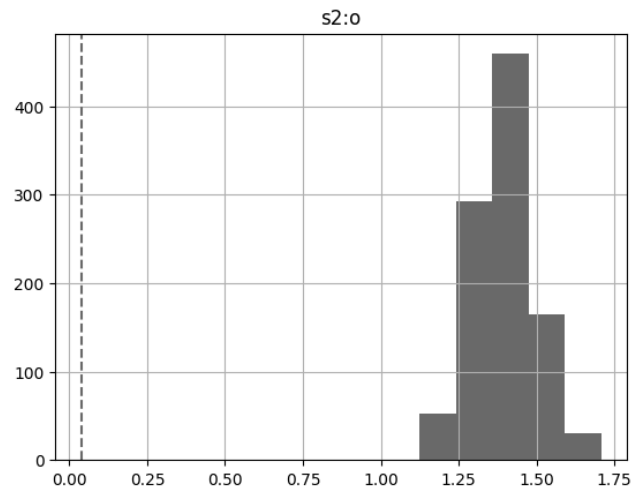


Figure 27: $H(o, C, N \Rightarrow V1)$

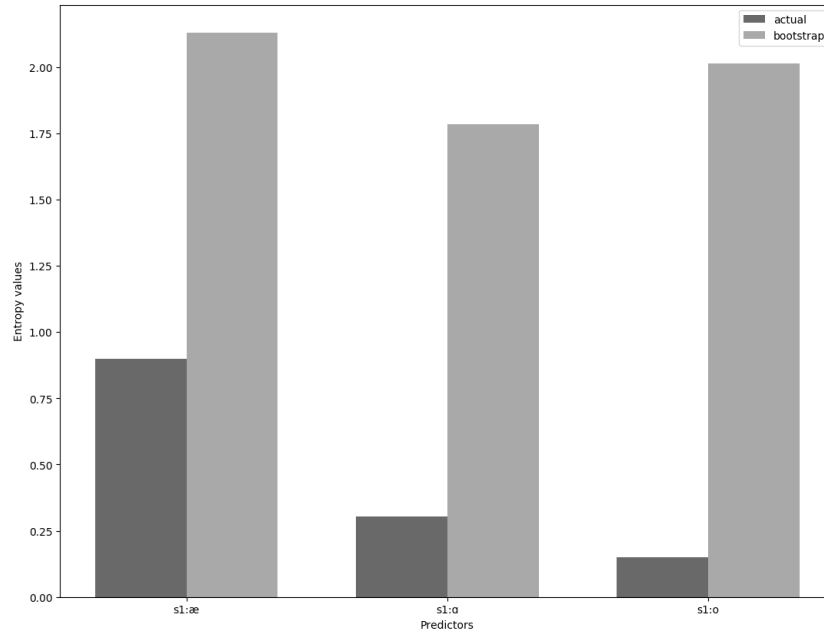


Figure 28: Comparison between mean entropies and observed ones (predicting V2)

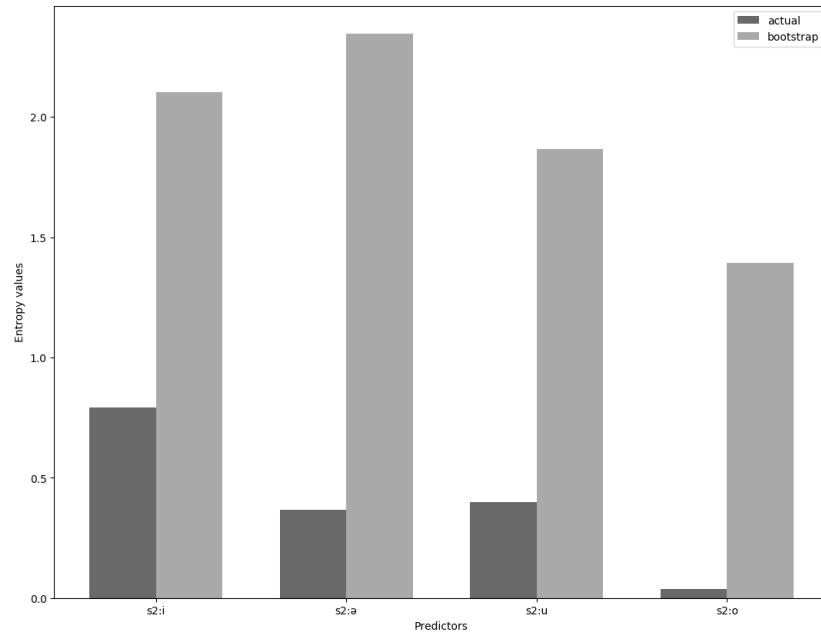


Figure 29: Comparison between mean entropies and observed ones (predicting V1)

4.2.2 Bootstrap results for ablauting verbs

Mean $H(\text{æ}, \text{coda}, \text{nativeness} \Rightarrow \text{v2})$: 1.3036801764658184

Variance: 0.007433756353992813

p -value = 0.0

Mean $H(\alpha, \text{coda}, \text{nativeness} \Rightarrow V2)$: 0.5899044566227523

Variance : 0.029026054196172657

p -value = 0.0

Mean $H(o, \text{coda}, \text{nativeness} \Rightarrow v2)$: 1.2308733184570546

Variance: 0.00892685115333458

p -value = 0.0

Mean $H(i, \text{coda}, \text{nativeness} \Rightarrow v1)$: 1.138650618414019

Variance: 0.00625896686984697

p -value = 0.0

Mean $H(\partial, \text{coda}, \text{nativeness} \Rightarrow v1)$: 0.6793517492920144

Variance: 0.018562048781324628

p -value = 0.003

Mean $H(u, \text{coda}, \text{nativeness} \Rightarrow v1)$: 0.9457955381209975

Variance: 0.011074385059152814

p -value = 0.0

Mean $H(o, \text{coda}, \text{nativeness} \Rightarrow v1)$: 0.0

Variance: 0.0

p -value = 0.0

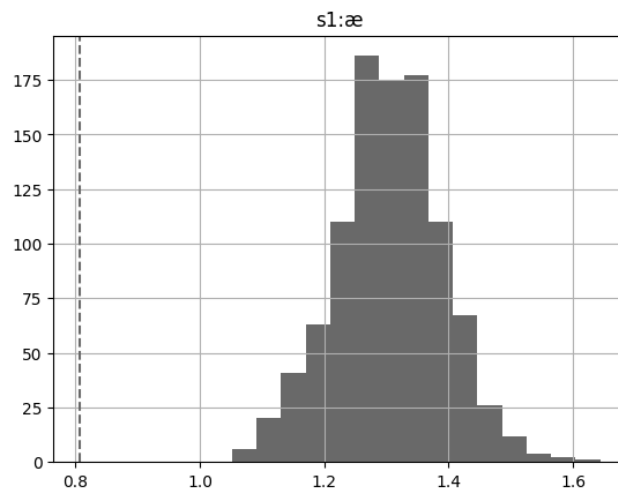


Figure 30: $H(\text{æ}, C, N \Rightarrow V2)$

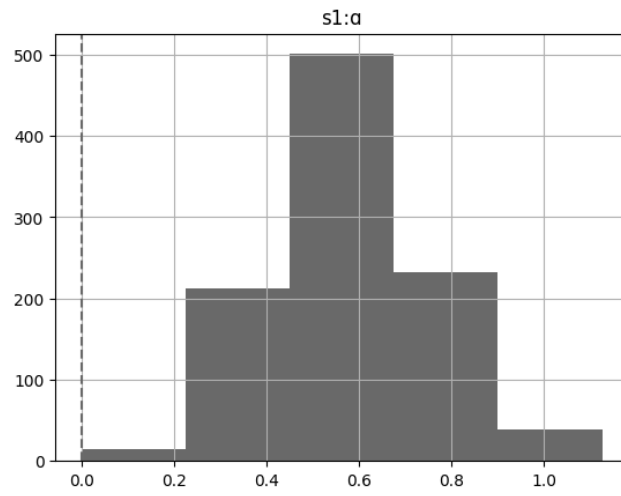


Figure 31: $H(a,C,N \Rightarrow V2)$

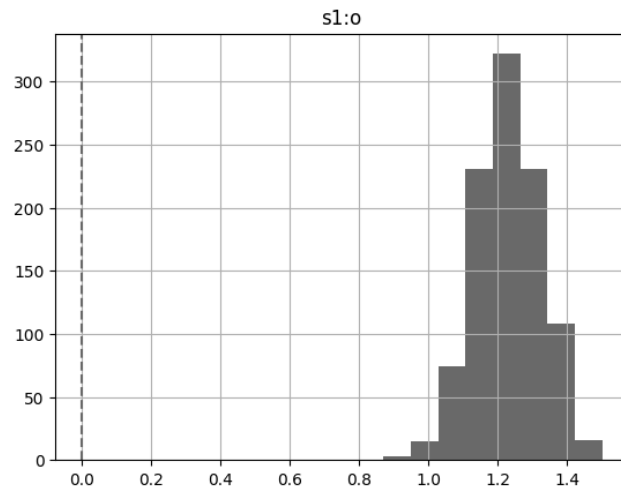


Figure 32: $H(o,C,N \Rightarrow V2)$

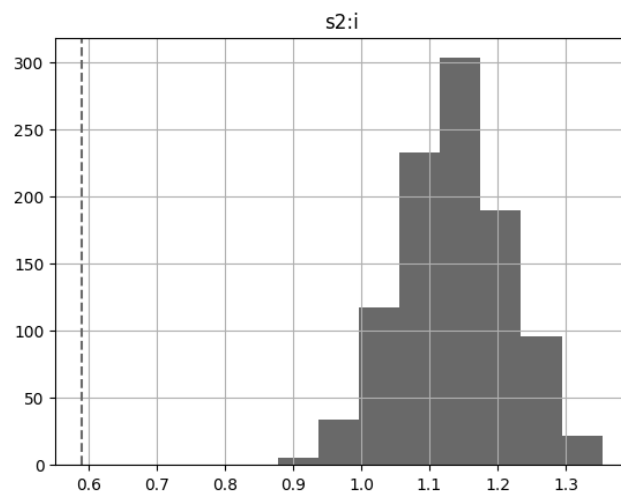


Figure 33: $H(i, C, N \Rightarrow V1)$

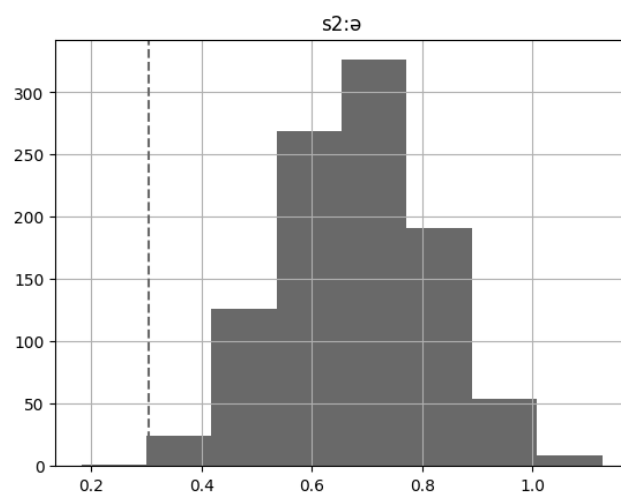


Figure 34: $H(ə, C, N \Rightarrow V1)$

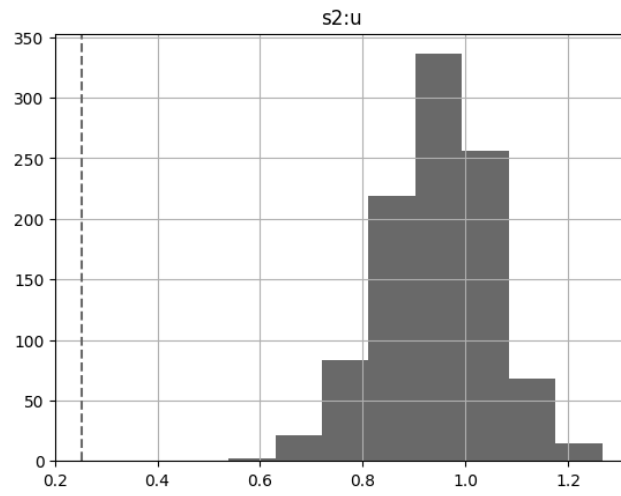


Figure 35: $H(u, C, N \Rightarrow V1)$

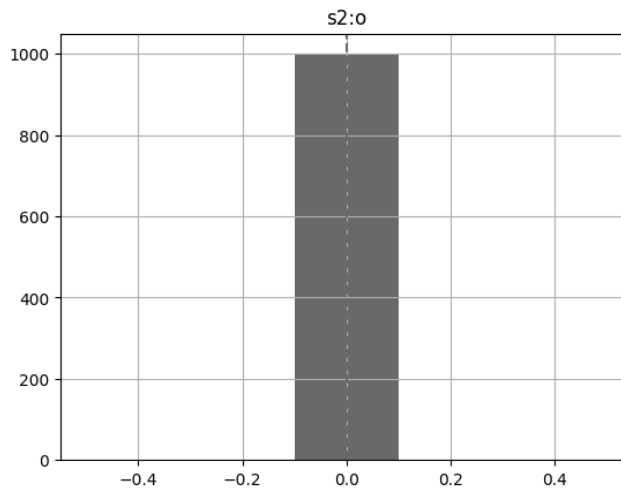


Figure 36: $H(o, C, N \Rightarrow V1)$

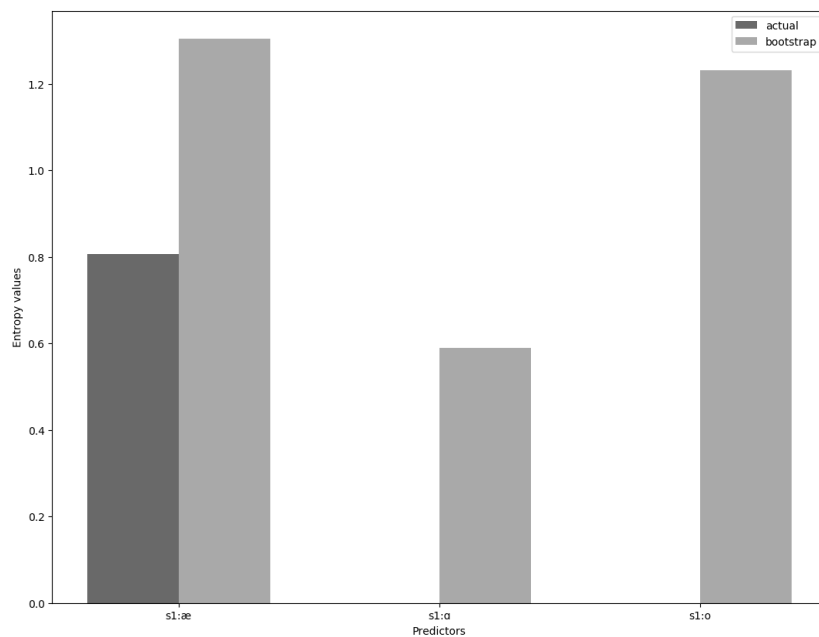


Figure 37: Comparison between mean entropies and observed ones (predicting V2)

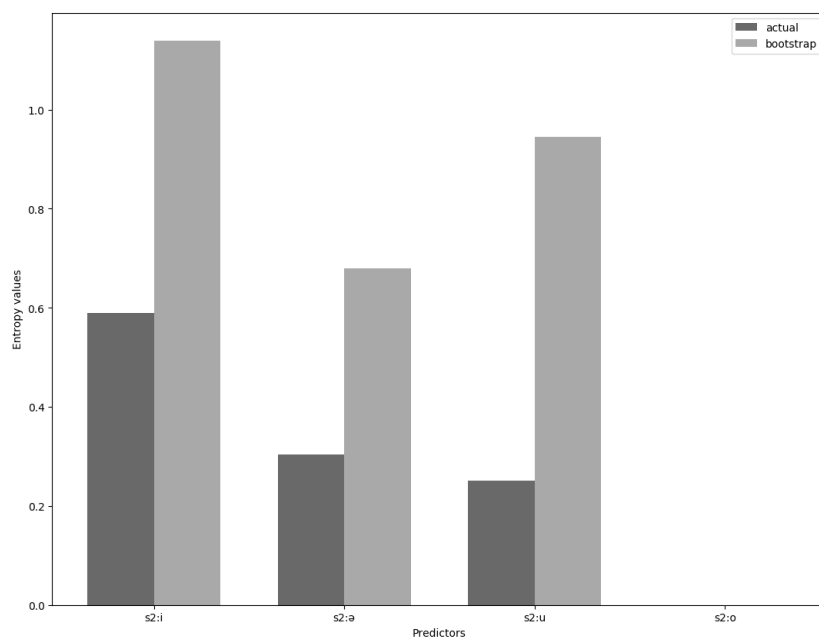


Figure 38: Comparison between mean entropies and observed ones (predicting V1)